



Intersectional fair ranking via subgroup divergence

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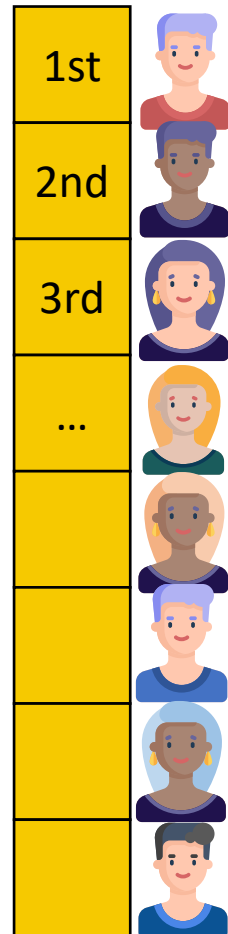
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di Torino



Rankings are adopted everywhere



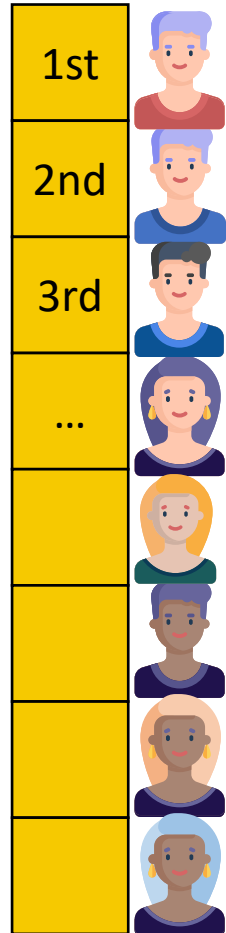
Internship access

University admissions

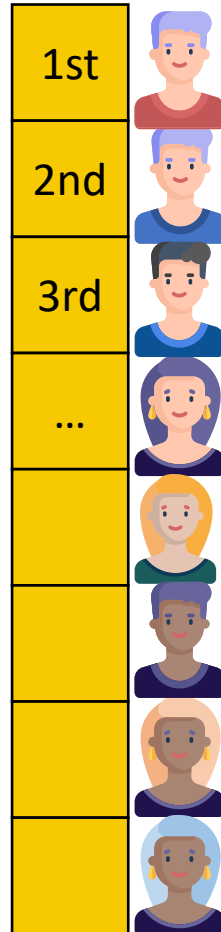
Job positions

Travel grants

Rankings are adopted everywhere



Rankings are adopted everywhere



Advantaged



Disadvantaged



Even more disadvantaged

↘ **Intersectionality**

Fair ranking – current approaches

A priori knowledge disadvantaged protected groups

Impose fairness constraints

At least X for each gender, at least Y for each ethnicity

Fair ranking – current approaches

A priori knowledge disadvantaged protected groups

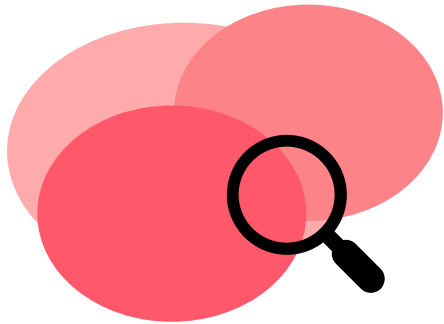
But.. which are the groups that need to be protected?

Impose fairness constraints

At least X for each gender, at least Y for each ethnicity

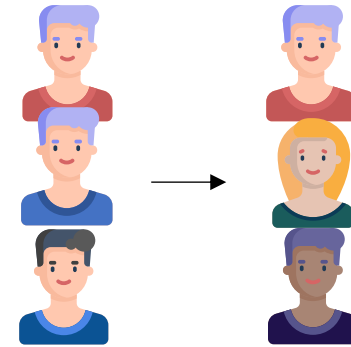
But.. how much representation is *enough*?

Our approach



Automatic identification of disadvantaged subgroups

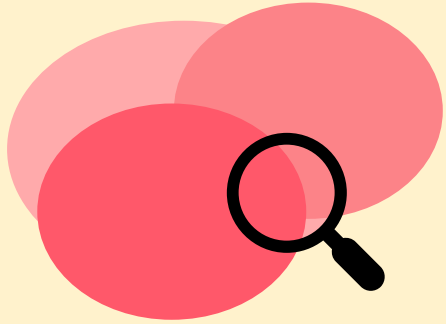
Via subgroup identification techniques



Mitigation of subgroup disadvantage

Based on their degree of disadvantage

Our approach



Automatic identification of disadvantaged subgroups

Via subgroup identification techniques



Automatic identification of disadvantaged subgroups



{gender=male ,
ethnicity=Cauc}



{gender=female}



{gender=female ,
ethnicity=Afr-Am}

- **Extract subgroups** over protected attributes via frequent pattern mining
 - Above frequency threshold to control the enumeration and statistical significance

Automatic identification of disadvantaged subgroups



{gender=male ,
ethnicity=Cauc}



{gender=female}



{gender=female ,
ethnicity=Afr-Am}

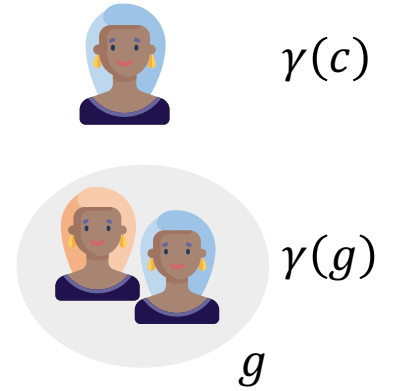
- **Extract subgroups** over protected attributes via frequent pattern mining
 - Above frequency threshold to control the enumeration and statistical significance
- **Compute their** degree of **disadvantage** (or advantage) in the ranking
 - Notion of subgroup divergence

Subgroup divergence Δ

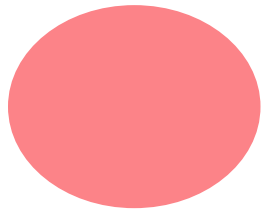
C : all candidates; g : a group;

$\gamma(c)$: **utility** of a candidate in the ranking, e.g., the score or ranking position

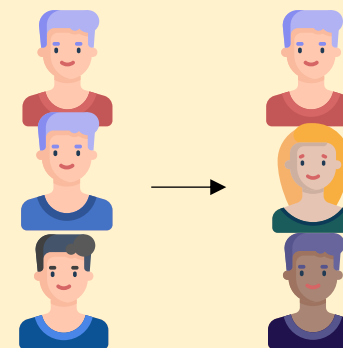
$\gamma(g)$: average utility of the candidates in group g



$$\Delta_{\gamma}(g) = \gamma(g) - \gamma(C)$$



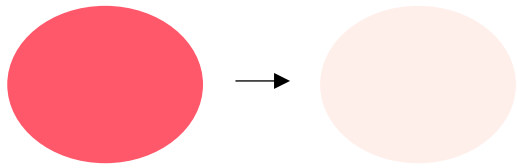
Disadvantaged group: $\Delta_{\gamma}(g) < 0$ & statistically significant



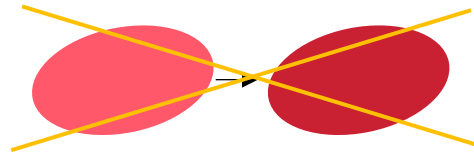
Mitigation of subgroup disadvantage

Based on their degree of disadvantage

Desired properties of the mitigation process



**Mitigate the divergence
of a subgroup g**

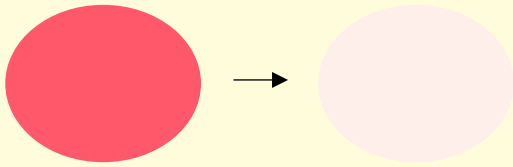


**Monotonicity
constraint**



**Constant average
overall behavior**

Desired properties of the mitigation process



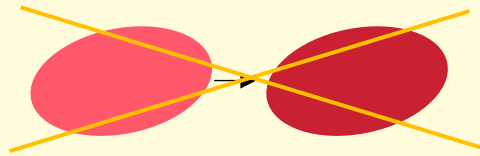
**Mitigate the divergence
of a subgroup g**

$$\Delta_{\gamma'}(g) > \Delta_{\gamma}(g)$$

Where γ' are the scores for the new ranking r

Reduce the disadvantage

Desired properties of the mitigation process



**Monotonicity
constraint**

$$\min_{g \in G} \Delta_{\gamma'}(g) > \min_{g \in G} \Delta_{\gamma}(g)$$

Avoid that by mitigating the divergence of a subgroup, we worsen the condition of others

Desired properties of the mitigation process



**Constant average
overall behavior**

$$\gamma(C) = \gamma'(C)$$

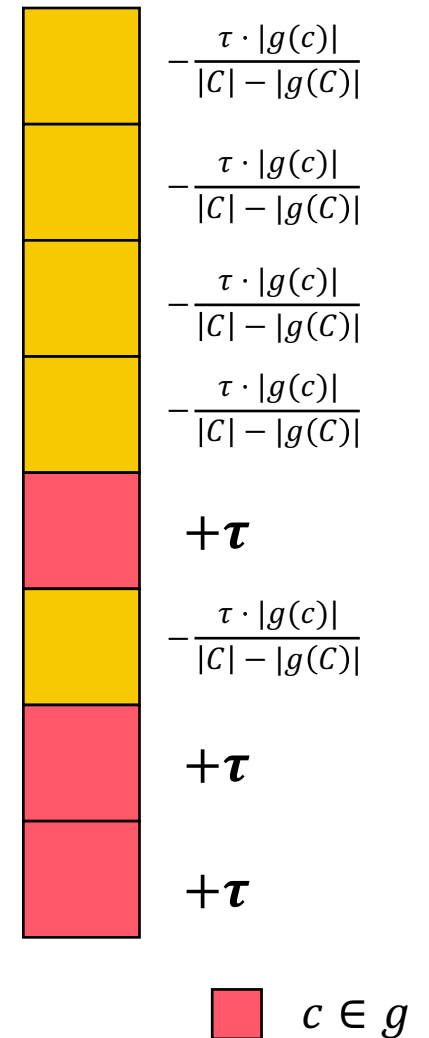
**Overall ranking utility is maintained in
the population**

Step of mitigation for disadvantage group g

Update the scores γ' of the candidates $c \in \mathcal{C}$ as follows

$$\gamma'(c) = \begin{cases} \gamma(c) + \tau & c \in g \\ \gamma(c) - \frac{\tau \cdot |g(c)|}{|\mathcal{C}| - |g(\mathcal{C})|} & c \notin g \end{cases}$$

with $\tau \in \mathbb{R}_{>0}$



Step of mitigation for disadvantage group g

Update the scores γ' of the candidates $c \in \mathcal{C}$ as follows

$$\gamma'(c) = \begin{cases} \gamma(c) + \tau & c \in g \\ \gamma(c) \cdot \frac{\tau \cdot |g(c)|}{|\mathcal{C}| - |g(\mathcal{C})|} & c \notin g \end{cases}$$

with $\tau \in \mathbb{R}_{>0}$

Counterbalance the increase of the scores
Satisfies **constant average overall behavior** property

Step of mitigation for disadvantage group g

Update the scores γ' of the candidates $c \in \mathcal{C}$ as follows

$$\gamma'(c) = \begin{cases} \gamma(c) + \tau & c \in g \\ \gamma(c) - \frac{\tau \cdot |g(c)|}{|\mathcal{C}| - |g(\mathcal{C})|} & c \notin g \end{cases}$$

with $\tau \in \mathbb{R}_{>0}$

For $\tau > 0$, $\gamma'(c) > \gamma(c) \rightarrow \Delta_{\gamma'}(g) > \Delta_{\gamma}(g)$

Implement the **mitigation of the divergence of a subgroup**



Step of mitigation for disadvantage group g

Update the scores γ' of the candidates $c \in \mathcal{C}$ as follows

$$\gamma'(c) = \begin{cases} \gamma(c) + \tau & c \in g \\ \gamma(c) - \frac{\tau \cdot |g(c)|}{|\mathcal{C}| - |g(\mathcal{C})|} & c \notin g \end{cases}$$

with $\tau \in \mathbb{R}_{>0}$



**Does it satisfy the monotonicity property?
... Depends on τ**

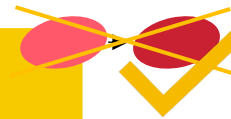
Ensuring the monotonicity property

For $c \notin g$, we decrease the score \rightarrow we want to avoid decreasing it such that

$$\min_{g \in G} \Delta_{\gamma}(g) > \min_{g \in G} \Delta_{\gamma'}(g)$$

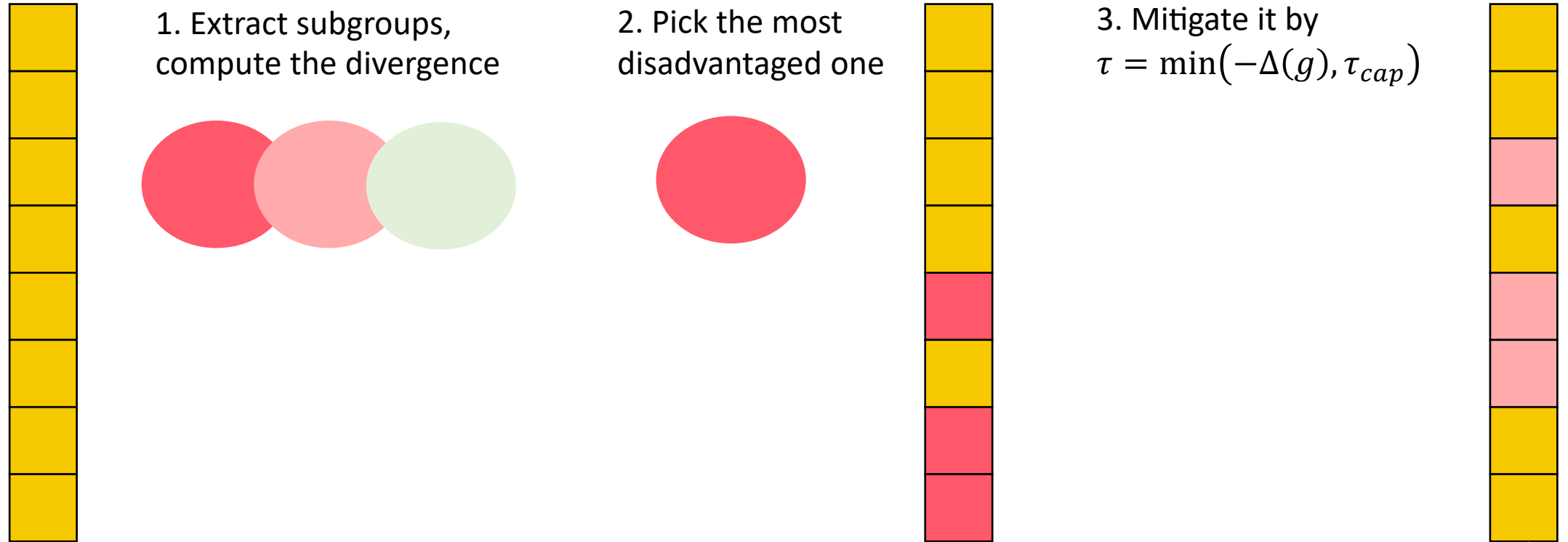
We compute the maximum supported τ_{cap} for all extracted subgroups

$$\tau = \min(-\Delta(g), \tau_{cap})$$



For a full mitigation

Iterative process



We repeat the mitigation step until

- No disadvantaged group
- No $\tau > 0$

Example for LSAT dataset

21,791 law students; we rank them by LSAT score

Gender and ethnicity as protected attributes

There are 11 disadvantage and 4 advantaged groups

Disadvantaged group	Highest position	50% by position	Δ
ethnicity=African-American, gender=female	777	20,163	-7,7
ethnicity=African-American	402	19,968	-7,35

Advantaged group	Highest position	50% by position	Δ
ethnicity=Caucasian, gender=male	1	9,690	0,96
ethnicity=Caucasian	1	10,028	0,76

Example for LSAT dataset - mitigation

Disadvantaged group	Δ_y
ethnicity=African-American, gender=female	-7,7
ethnicity=African-American	-7,35

Advantaged group	Δ_y
ethnicity=Caucasian, gender=male	0,96
ethnicity=Caucasian	0,76

Example for LSAT dataset - mitigation

Disadvantaged group	Δ_γ	$\Delta_{\gamma'}$ 1st iteration
ethnicity=African-American, gender=female	-7,7	0
ethnicity=African-American	-7,35	-2,66

Advantaged group	Δ_γ	$\Delta_{\gamma'}$ 1st iteration
ethnicity=Caucasian, gender=male	0,96	0,67
ethnicity=Caucasian	0,76	0,46

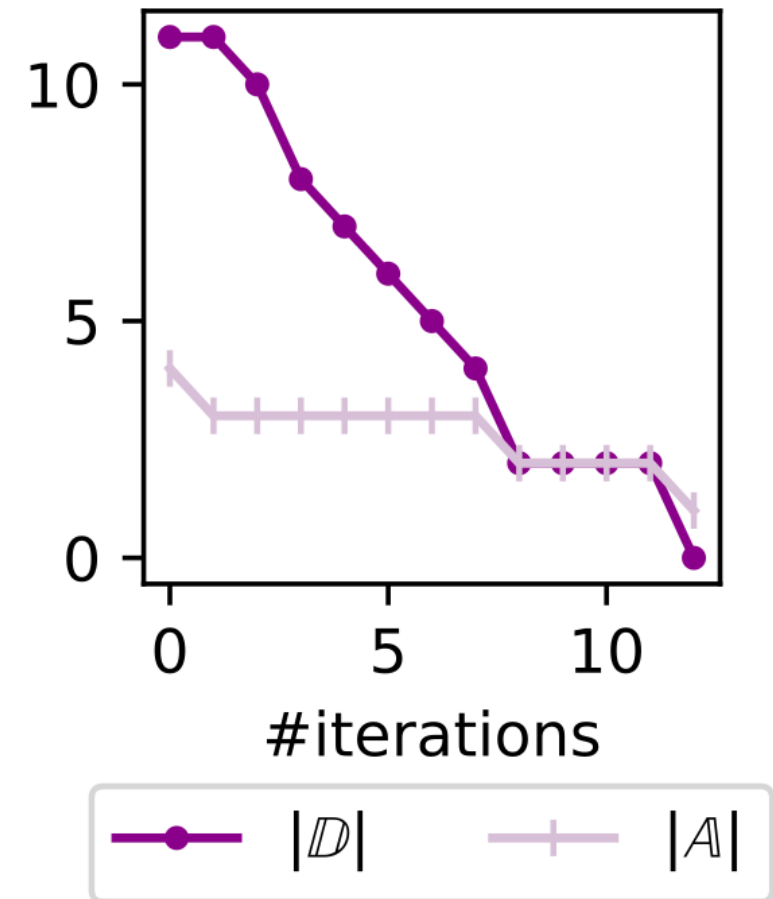
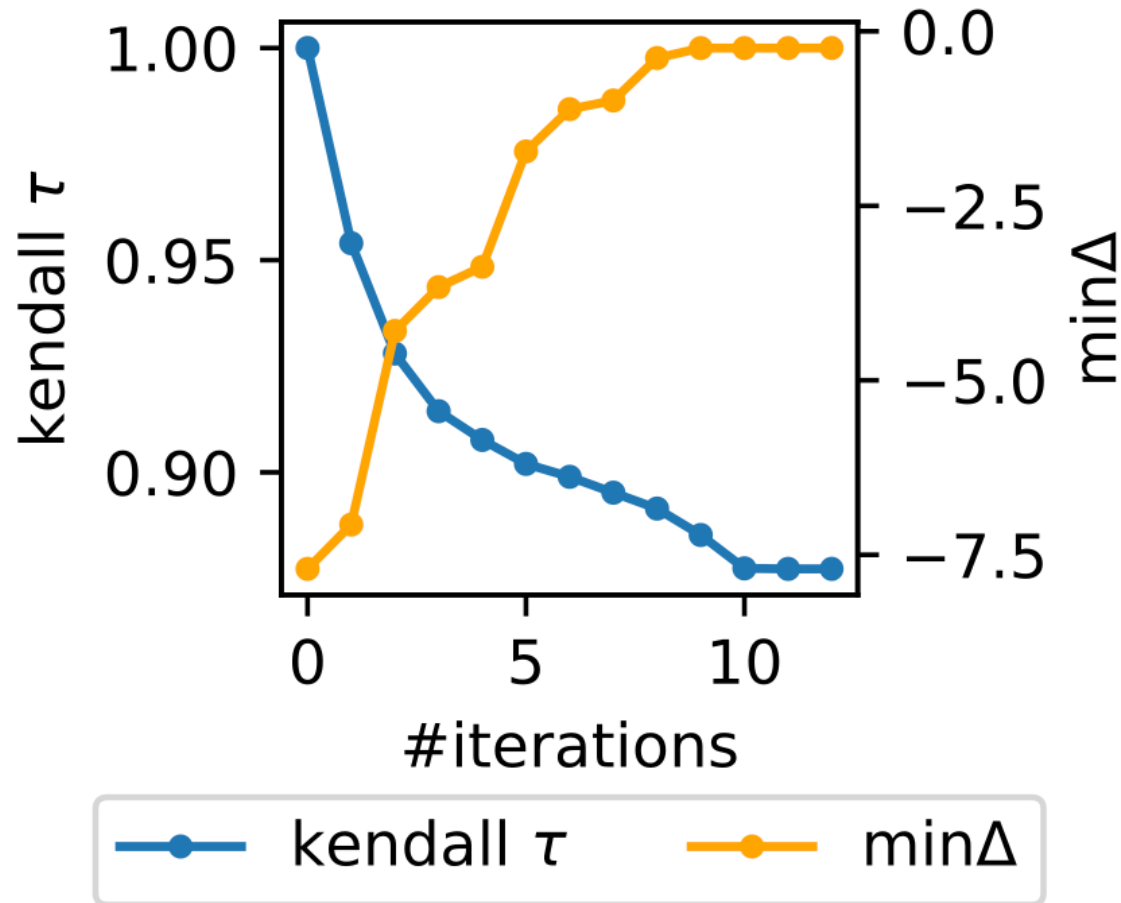
Example for LSAT dataset - mitigation

Disadvantaged group	Δ_γ	$\Delta_{\gamma'}$ 1 st iteration	$\Delta_{\gamma'}$ mitigation
ethnicity=African-American, gender=female	-7,7	0	0,15
ethnicity=African-American	-7,35	-2,66	0,02

Advantaged group	Δ_γ	$\Delta_{\gamma'}$ 1 st iteration	$\Delta_{\gamma'}$ mitigation
ethnicity=Caucasian, gender=male	0,96	0,67	0,15
ethnicity=Caucasian	0,76	0,46	0,06

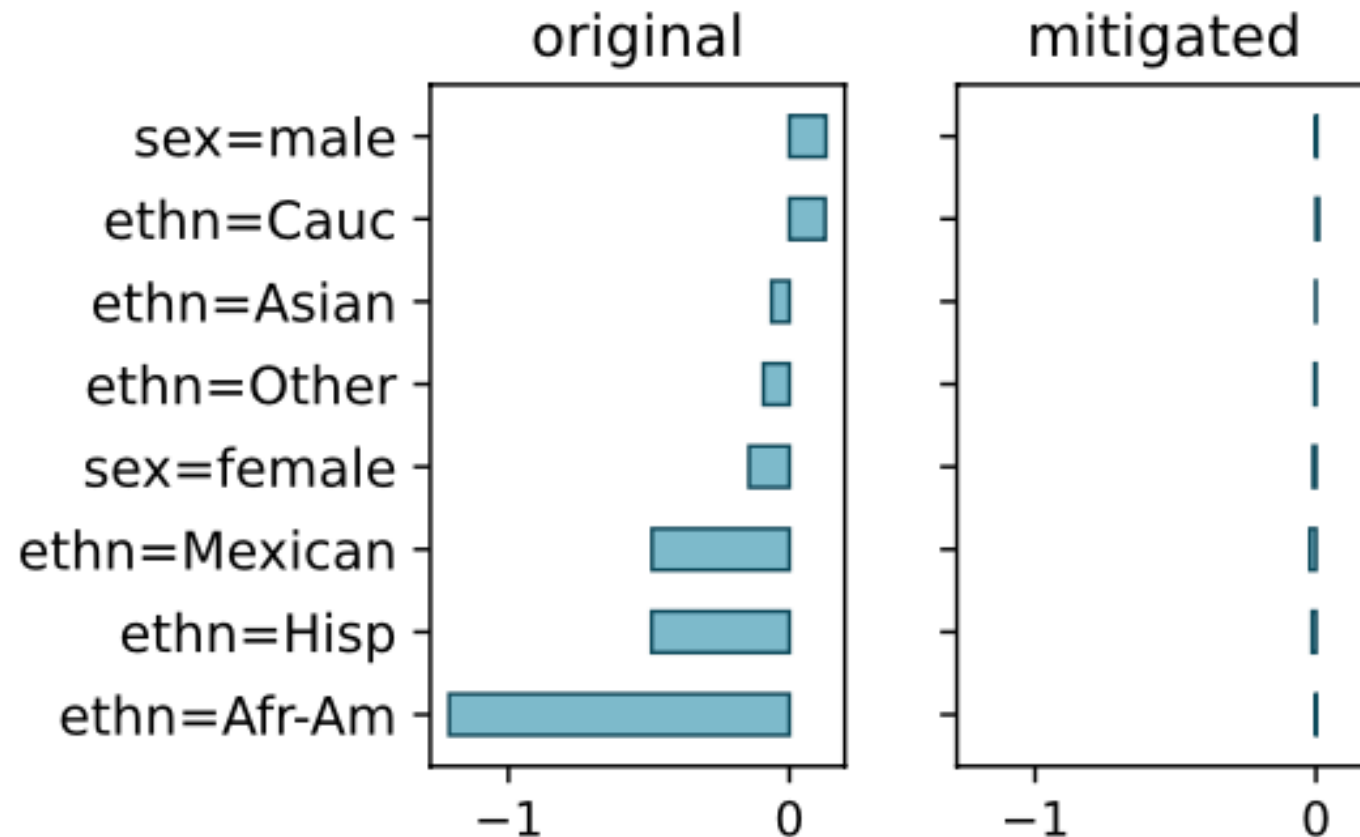
Example for LSAT dataset – impact of mitigation

Min disadvantage, closeness to original ranking, dis&advantage groups



Example for LSAT dataset – impact of mitigation

Contribution to the divergence via Global Shapley value



Outline of the experimental results

5 **real-world** (LSAT, COMPAS, folktables, german credit, IIT-JEE) + 1 **synthetic datasets**
3 **baseline approaches** – also addressing intersectionality

Our approach always mitigates the disadvantages,
reducing disadvantaged subgroups to 0 **with high**
closeness to the original ranking

THANK YOU!



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